

Quiz 13

$$1. f = x^3 + x^2y^3 + 2z^3y^4 + z^3 = 5$$

$$\nabla f = \langle 3x^2 + 2xy^3, 3x^2y^2 + 8z^3y^3, 6z^2y^4 + 3z^2 \rangle$$

$$\nabla f(1,1,1) = \langle 5, 11, 9 \rangle$$

$$\langle x-1, y-1, z-1 \rangle \cdot \langle 5, 11, 9 \rangle = 0 \Rightarrow$$

$$5x + 11y + 9z = 25$$

$$2. g = 4x + e^{2xy} + y^2 - z = 0$$

$$\nabla g = \langle 4 + 2ye^{2xy}, 2xe^{2xy} + 2y, -1 \rangle$$

$$\nabla g(0, 2, 5) = \langle 8, 4, -1 \rangle$$

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 8t \\ 2 + 4t \\ 5 - t \end{pmatrix}.$$