

Quiz 6



(a) $r=2y$, so cross section

Area is $\pi r^2 = \pi (2y)^2 = 4\pi y^2$

distance is $3-y$

endpoints $0 \leq y \leq 2$

$$\begin{aligned} \therefore W &= \int_0^2 (40) \cdot 4\pi y^2 (3-y) dy = 160\pi \int_0^2 (3y^2 - y^3) dy \\ &= 160\pi \left(y^3 - \frac{y^4}{4} \right)_0^2 = 160\pi (8-4) = 640\pi \text{ ft-lbs} \end{aligned}$$

(b) distance $= 3-y+15 = 18-y$

$$\text{so } W = \int_0^2 (40) 4\pi y^2 (18-y) dy$$