

## Homework # 8 (Due Monday, February 24)

- Read pp. 51-58.
- Need to know: Thm 7.1 (Statement),  
Thm 7.2 and 7.3 (Statements and proofs),  
Proposition 7.1 (Statement and proof)

Do the following problems:

1. Factor  $x^7 - 1$  as a product of linear and/or quadratic polynomials with real coefficients.
2. Write down an equation in the form  $a_4 x^4 + a_3 x^3 + a_2 x^2 + a_1 x + a_0 = 0$  with real coefficients, so that this equation has roots  $x_1 = 1 - i$  and  $x_2 = 1 + 3i$ .
3. If the roots of the equation  $x^3 - 3x + 1 = 0$  are  $\alpha, \beta, \gamma$ , find another cubic equation whose roots are
  - a)  $\alpha^2, \beta^2, \text{ and } \gamma^2$ .
  - b)  $\frac{1}{\alpha}, \frac{1}{\beta}, \frac{1}{\gamma}$ .