## HOMEWORK 23 DIFFERENTIAL EQUATIONS DUE 10-31

## Show your work!

- (1) Two objects, one at 50 °C and one at 100 °C, are placed in a room together. The rate of change of the temperature of each object is proportional, but opposite, to the amount by which its temperature exceeds the temperature of the other object.
  - (a) Suppose that the temperature of the initially cooler object is initially increasing at 2 °C/s, whereas the temperature of the initially warmer object is initially decreasing at 1 °C/s. Model this situation with differential equations. Your equations should involve no undetermined constants.
  - (b) What are the limits of the temperatures of the initially cooler object, and the initially warmer object, as  $t \to \infty$ ? (Don't just guess; you should solve your differential equations from (a).)
- (2) Consider the overdamped harmonic oscillator from class, with mass m = 1 kg, spring constant  $k = 10 \frac{\text{N}}{\text{m}}$ , and damping coefficient  $b = 7 \frac{\text{N}}{\text{m/s}}$ .
  - (a) Is it possible for a solution to *never* cross the rest position x = 0 for any t-value (positive or negative)? Give an example (with no undetermined constants), or explain why not.
  - (b) Is it possible for a solution to cross the rest position x = 0 for *exactly one t*-value (positive or negative)? Give an example (with no undetermined constants), or explain why not.
  - (c) Is it possible for a non-0 solution to cross the rest position x = 0 for more than one *t*-value (positive or negative)? Give an example (with no undetermined constants), or explain why not.
  - Three book problems: #3.5.19; #3.6.10, 32.