

**HOMEWORK 9**  
**CALCULUS III**  
**DUE 02-18**

(1) Let  $\vec{u}$  and  $\vec{v}$  be any two vectors with  $\vec{u} \neq \vec{0}$ . We want to show that we can write

$$\vec{v} = \vec{v}_{\parallel} + \vec{v}_{\perp},$$

where  $\vec{v}_{\parallel}$  is parallel to  $\vec{u}$ , and  $\vec{v}_{\perp}$  is orthogonal to  $\vec{u}$ .

- (a) How can you express algebraically (*i.e.*, in terms of vector operations) that  $\vec{v}_{\parallel}$  is parallel to  $\vec{u}$ ?
  - (b) How can you express algebraically that  $\vec{v}_{\perp}$  is orthogonal to  $\vec{u}$ ?
  - (c) Use your answers to (a) and (b) to find a formula for  $\vec{u} \cdot \vec{v}$ .
  - (d) Use your answers to (a) and (c) to find a formula for  $\vec{v}_{\parallel}$ .
  - (e) Use your answer to (d) to show that  $\vec{u}$  is orthogonal to  $\vec{v} - \vec{v}_{\parallel}$ .
- **Eleven** book problems: #11.3.15, 22, 24, 29, 30, 42, 44, 47, 56, 71, 73. For #11.3.42, you know  $\text{proj}_{\vec{OA}} \vec{w}$ , where  $\vec{w}$  is the weight of the load. How can you use it to find  $\|\vec{w}\|$ ? For #11.3.73, you will need the formula for work on p. 789.