## HOMEWORK 6 DISCRETE MATHEMATICS I DUE 02-07

## Show your work!

(1) For this problem, the universe of discourse for $x$ is "people in this class". There are twelve people in this class: Daniel, Alexis, Jackie, Ashlee, David, Nguyen, Alissa, Amy, Ronnie, Aakash, Pat, and James.
(a) Write a statement that is logically equivalent to $\forall x . P(x)$ but that does not use quantifiers.
(b) Write a statement that is logically equivalent to $\exists x . P(x)$ but that does not use quantifiers.
(2) Explain your answers.
(a) Suppose that the universe of discourse for $x$ consists of exactly one object. What is the relationship between the statements $\forall x . P(x)$ and $\exists x . P(x)$ ?
(b) Suppose that the universe of discourse for $x$ has no objects; that is, that it is empty. Is $\forall x . P(x)$ true or false? Is $\exists x . P(x)$ true or false?

- Eight book problems: \#1.3.14, 15, 21, 45, 47, 48, 49, 50.

