HOMEWORK 11 APPLIED CALCULUS DUE 2013-10-03

Show your work!

- (1) (a) In your own words, explain why, when y' is positive and y'' is negative, it means that y is increasing slower. Draw a picture of such a function y.
 - (b) In your own words, explain why, when y' is negative and y'' is negative, it means that y is decreasing faster. Draw a picture of such a function y.
- (2) Consider the function $f(x) = xe^x$.
 - (a) Compute the first derivative f'(x), and make a sign diagram for it.
 - (b) Compute the second derivative f''(x), and make a sign diagram for it.
 - (c) Use your sign diagrams from (a) and (b), and the fact that the only x-intercept of y = f(x) is at x = 0, to sketch a picture of the graph of y = f(x).
- (3) Consider the function $g(x) = e^{-x^2}$.
 - (a) Compute the first derivative g'(x), and make a sign diagram for it.
 - (b) Compute the second derivative g''(x), and make a sign diagram for it.
 - (c) Use your sign diagrams from (a) and (b), and the fact that g(x) is always positive, to sketch a picture of the graph of y = g(x).
 - Seven book problems: #12.2.20, 27, 31, 33, 51, 52, 61.