2017 Calculus Bee
Wednesday, April 26, 2016

| 1st Place | Thinh Doan |
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| 2nd Place | Clark Mask |
| 3rd Place | Bao Thach |

(1) Find the derivative of the function $g(p)=p \sqrt{2017-p}$.
(2) Find $\lim _{x \rightarrow \infty} \frac{2017 x-x^{2017}}{x^{2017}+2017 x}$.
(3) Below is the graph of $y=\frac{d F}{d x}$.

(a) Find $F^{\prime \prime}(2)$.
(b) If $F(-1)=2017$, find $F(4)$.
(4) Find the maximum value of the function $F(x)=x(2017-x)$.
(5) Put the following quantities in increasing order.
(A) $\int_{-\pi}^{\pi} \sin ^{4}\left(x^{6}\right) d x$.
(B) $\int_{-\pi}^{\pi} \sin ^{6}\left(x^{6}\right) d x$.
(C) $\int_{-\pi}^{\pi} e^{x^{2}} \sin ^{4}\left(x^{6}\right) d x$.
(D) $\int_{-\pi}^{\pi} \sin ^{2017}\left(x^{2017}\right) d x$.
(6) Find the approximate value of $\sum_{k=1}^{2017} \frac{2017}{3^{k}}$, accurate to within 0.01 .
(7) Evaluate

$$
\int \frac{\ln x}{x} d x
$$

